

Question		Answer	Marks	Guidance	
1	(i)	$y' = 3x^2 - 5$ their $y' = 0$ (1.3, -4.3) cao (-1.3, 4.3) cao	M1 M1 A1 A1 [4]	or A1 for $x = \pm\sqrt{\frac{5}{3}}$ oe soi allow if not written as co-ordinates if pairing is clear	ignore any work relating to second derivative
1	(ii)	crosses axes at (0, 0) and $(\pm\sqrt{5}, 0)$ sketch of cubic with turning points in correct quadrants and of correct orientation and passing through origin x-intercepts $\pm\sqrt{5}$ marked	B1 B1 B1 B1 [4]	condone x and y intercepts not written as co-ordinates; may be on graph $\pm(2.23 \text{ to } 2.24)$ implies $\pm\sqrt{5}$ may be in decimal form ($\pm 2.2\dots$)	See examples in Appendix must meet the x-axis three times B0 eg if more than 1 point of inflection
1	(iii)	substitution of $x = 1$ in $f'(x) = 3x^2 - 5$ -2 $y - -4 = (\text{their } f'(1)) \times (x - 1)$ oe $-2x - 2 = x^3 - 5x$ and completion to given result www use of Factor theorem in $x^3 - 3x + 2$ with -1 or ± 2 $x = -2$ obtained correctly	M1 A1 M1* M1dep* M1 A1 [6]	or $-4 = -2 \times (1) + c$ or any other valid method; must be shown	sight of -2 does not necessarily imply M1: check $f'(x) = 3x^2 - 5$ is correct in part (i) eg long division or comparing coefficients to find $(x - 1)(x^2 + x - 2)$ or $(x + 2)(x^2 - 2x + 1)$ is enough for M1 with both factors correct NB M0A0 for $x(x^2 - 3) = -2$ so $x = -2$ or $x^2 - 3 = -2$ oe

2	i	$(x+5)(x-2)(x+2)$	2	M1 for a $(x+5)(x-2)(x+2)$	2
	ii	$[(x+2)](x^2+3x-10)$	M1	for correct expansion of one pair of their brackets	2
		$x^3+3x^2-10x+2x^2+6x-20$ o.	M1	for clear expansion of correct factors – accept given answer from $(x+5)(x^2-4)$ as first step	
	iii	$y' = 3x^2 + 10x - 4$ their $3x^2 + 10x - 4 = 0$ s.o.i. $x = 0.36\dots$ from formula o.e.	M2 M1 A1	M1 if one error or M1 for substitution of 0.4 if trying to obtain 0, and A1 for correct demonstration of sign change	6 2
$(-3.7, 12.6)$		B1+1			
iv	$(-1.8, 12.6)$	B1+1	accept $(-1.9, 12.6)$ or f.t. ($\frac{1}{2}$ their max x, their max y)		

3	(i)	$3x^2 - 6x - 9$	M1	c.a.o.	6
		use of their $y' = 0$ $x = -1$ $x = 3$ valid method for determining nature of turning point max at $x = -1$ and min at $x = 3$	M1 A1 A1 M1 A1		
	(ii)	$x(x^2 - 3x - 9)$ $\frac{3 \pm \sqrt{45}}{2}$ or $(x - \frac{3}{2})^2 = 9 + \frac{9}{4}$ $0, \frac{3}{2} \pm \frac{\sqrt{45}}{2}$ o.e.	M1 M1 A1		3
(iii)	sketch of cubic with two turning points correct way up x-intercepts – negative, 0, positive shown	G1 DG1	2		

4	i	$y' = 6x^2 - 18x + 12$ $= 12$ $y = 7$ when $x = 3$ tgt is $y - 7 = 12(x - 3)$ verifying $(-1, -41)$ on tgt	M1 M1 B1 M1 A1	condone one error subst of $x = 3$ in <u>their</u> y' f.t. their y and y' or B2 for showing line joining $(3, 7)$ and $(-1, -41)$ has gradient 12	5
	ii	$y' = 0$ soi quadratic with 3 terms $x = 1$ or 2 $y = 3$ or 2	M1 M1 A1 A1	Their y' Any valid attempt at solution or A1 for $(1, 3)$ and A1 for $(2, 2)$ marking to benefit of candidate	4
	iii	cubic curve correct orientation touching x- axis only at $(0.2, 0)$ max and min correct curve crossing y axis only at -2	G1 G1 G1	f.	3

5	i	$y' = 6 - 2x$ $y' = 0$ used $x = 3$ $y = 16$ $(0, 7)$ $(-1, 0)$ and $(7, 0)$ found or marked on graph sketch of correct shape	M1 M1 A1 A1 3 1	condone one error 1 each must reach pos. y - axis	8
	ii	58.6 to 58.7	3 M1	B1 for $7x + 3x^2 - x^3/3$ [their value at 5] - [their value at 1] dependent on integration attempted	3
	iii	using his (ii) and 48	1		1